



*Indirect estimation
of labour market characteristics
in the functional areas of provincial capitals*

Tomasz Józefowski^{1,2}, Kamil Wilak^{1,2}

¹ Statistical Office in Poznań

² Poznań University of Economics and Business, Poland

Poznań, 18-19.11.2024

Plan prezentacji

Introduction

Methodology

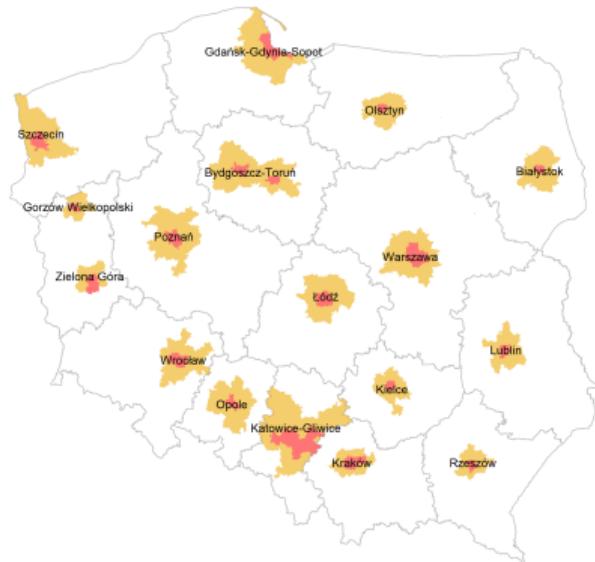
Empirical study

Conclusions

Literature

Introduction

Functional urban areas of provincial capital cities selected for Integrated Territorial Investments (ITI) in the period 2014-2020



Introduction

Aims

- ▶ Estimation of labour market indicators in functional urban areas of provincial capital cities.
- ▶ Use of SPREE-type estimators to improve estimation quality.

Motivation

- ▶ Growing information needs of data users.
- ▶ Limitations of the direct estimator.
- ▶ Costs of sample surveys.
- ▶ The need to reduce the respondent burden.
- ▶ Established literature on indirect estimation.
- ▶ Practical applications of SPREE.



Methodology

- ▶ Structure Preserving Estimators (SPREE) are a generalised class of synthetic estimators, i.e. those that rely on information from direct estimates.
- ▶ SPREE estimators can be used to estimate totals for small areas during intercensal periods or for more detailed domains.



Methodology

	Domain 1	Domain 2	...	Domain K	
Area 1	X_{11}	X_{12}	...	X_{1K}	$Y_{1.}$
Area 2	X_{21}	X_{22}	...	X_{2K}	$Y_{2.}$
⋮	⋮	⋮	⋮	⋮	⋮
Area A	X_{A1}	X_{A2}	...	X_{AK}	$Y_{A.}$
	$Y_{.1}$	$Y_{.2}$...	$Y_{.K}$	

- ▶ SPREE estimators rely on adjusted counts within the contingency table, obtained by applying the Iterative Proportional Fitting (IPF) method, so that they add up to known marginal totals.
- ▶ Input counts $X_{a,k}$ inside the contingency table can come from a census or an administrative register, while reliable direct estimates from a survey (e.g. LFS) are used as marginal totals $Y_{a.}$ and $Y_{.k}$ ($a = 1, \dots, A, k = 1, \dots, K$).

Methodology

- ▶ Y_{ak}, X_{ak} – denote values of the response variable and the proxy variable in a cell of a two-way contingency table, where a denotes the identifier of a small area, while j denotes levels of the grouping variable.
- ▶ Let $\log Y_{ak}, \log X_{ak}$ be expressed by a log-linear model:

$$\log Y_{ak} = \alpha_0^Y + \alpha_a^Y + \alpha_k^Y + \alpha_{ak}^Y, \quad (1)$$

$$\log X_{ak} = \alpha_0^X + \alpha_a^X + \alpha_k^X + \alpha_{ak}^X, \quad (2)$$

where:

- ▶ $\alpha_0^Y = \frac{1}{AK} \sum_a \sum_k \log Y_{ak}$ – general effect,
- ▶ $\alpha_a^Y = \frac{1}{K} \sum_k \log Y_{ak} - \alpha_0^Y$ – effect of area a ,
- ▶ $\alpha_k^Y = \frac{1}{A} \sum_a \log Y_{ak} - \alpha_0^Y$ – effect of k -th level of the grouping variable,
- ▶ $\alpha_{ak}^Y = \log Y_{ak} - \alpha_a^Y - \alpha_k^Y - \alpha_0^Y$ – interaction effect,

for $a = 1, \dots, A$ and $k = 1, \dots, k$.



Methodology

- ▶ SPREE estimator is based on the assumption that:

$$\alpha_{aj}^Y = \alpha_{ak}^X. \quad (3)$$

- ▶ Assumption (3) can be relaxed by using a GLSM model and adopting the assumption about the existence of a proportional relationship between association structures of the response variable and the proxy variable. In this way we obtain a generalised SPREE (GSPREE):

$$\alpha_{ak}^Y = \beta \alpha_{ak}^X. \quad (4)$$

- ▶ The literature provides other modifications of this estimator as well as their applications.

Empirical study

- ▶ **Data:**
 - aggregated statistical data based on administrative registers (2017),
 - Labour Force Survey (2017);
- ▶ **Domain:**
 - functional urban areas of provincial capital cities broken down by: (1) sex, (2) age groups (mobility age, non-mobility age);
- ▶ **Estimated parameter:**
 - the number of employed, unemployed and economically inactive persons,
 - labour market indicators: economic activity rate, employment rate, unemployment rate;
- ▶ **Association structure:**
 - counts obtained from aggregated statistical data based on administrative registers,
- ▶ **Allocation structure:**
 - LFS-based direct estimates of marginal totals in the target contingency table;
- ▶ **Methods:**
 - CAL , $SPREE_{2,L}$, $SPREE_{3,L}$, $GLSM_{2,L}$, $GLSM_{3S,L}$.



Empirical study

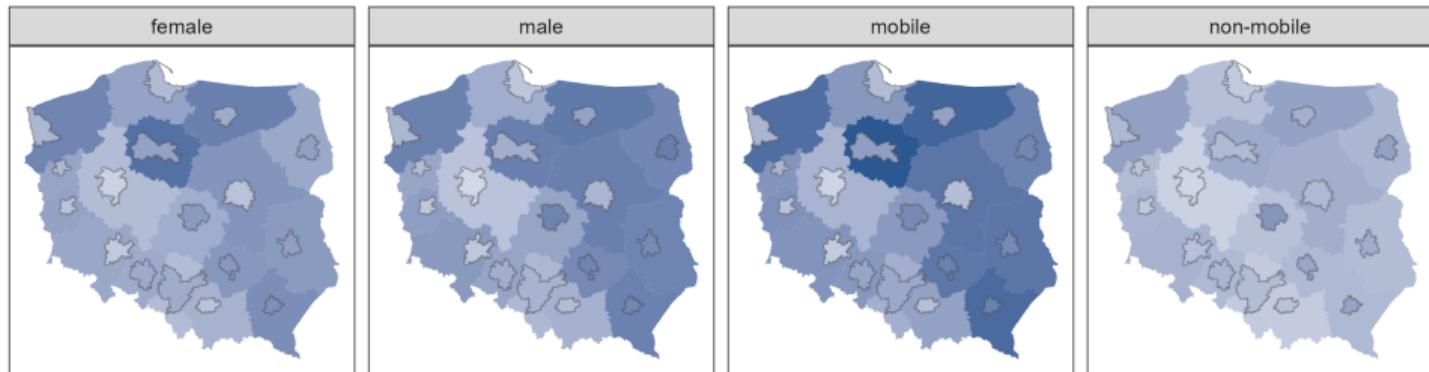
One of the association-allocation structures used in the empirical study.

	Functional urban area			Other parts of the province			
	employed	unemployed	inactive	employed	unemployed	inactive	
mobility-age							
dolnośląskie	$X_{1,1}$	$X_{1,2}$	$X_{1,3}$	$X_{1,4}$	$X_{1,5}$	$X_{1,6}$	$Y_{1,..}$
kujawsko-pomorskie	$X_{2,1}$	$X_{2,2}$	$X_{2,3}$	$X_{2,4}$	$X_{2,5}$	$X_{2,6}$	$Y_{2,..}$
⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮
zachodniopomorskie	$X_{16,1}$	$X_{16,2}$	$X_{16,3}$	$X_{16,4}$	$X_{16,5}$	$X_{16,6}$	$Y_{16,..}$
non-mobility age							
dolnośląskie	$X_{17,1}$	$X_{17,2}$	$X_{17,3}$	$X_{17,4}$	$X_{17,5}$	$X_{17,6}$	$Y_{17,..}$
kujawsko-pomorskie	$X_{18,1}$	$X_{18,2}$	$X_{18,3}$	$X_{18,4}$	$X_{18,5}$	$X_{18,6}$	$Y_{18,..}$
⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮
zachodniopomorskie	$X_{32,1}$	$X_{32,2}$	$X_{32,3}$	$X_{32,4}$	$X_{32,5}$	$X_{32,6}$	$Y_{32,..}$
	$Y_{.,1}$	$Y_{.,2}$	$Y_{.,3}$	$Y_{.,4}$	$Y_{.,5}$	$Y_{.,6}$	



Empirical study

SPREE estimates of the unemployment rate in functional urban areas of provincial capital cities and the remaining parts of the provinces, 2017



8
6
4
2
0

Conclusions

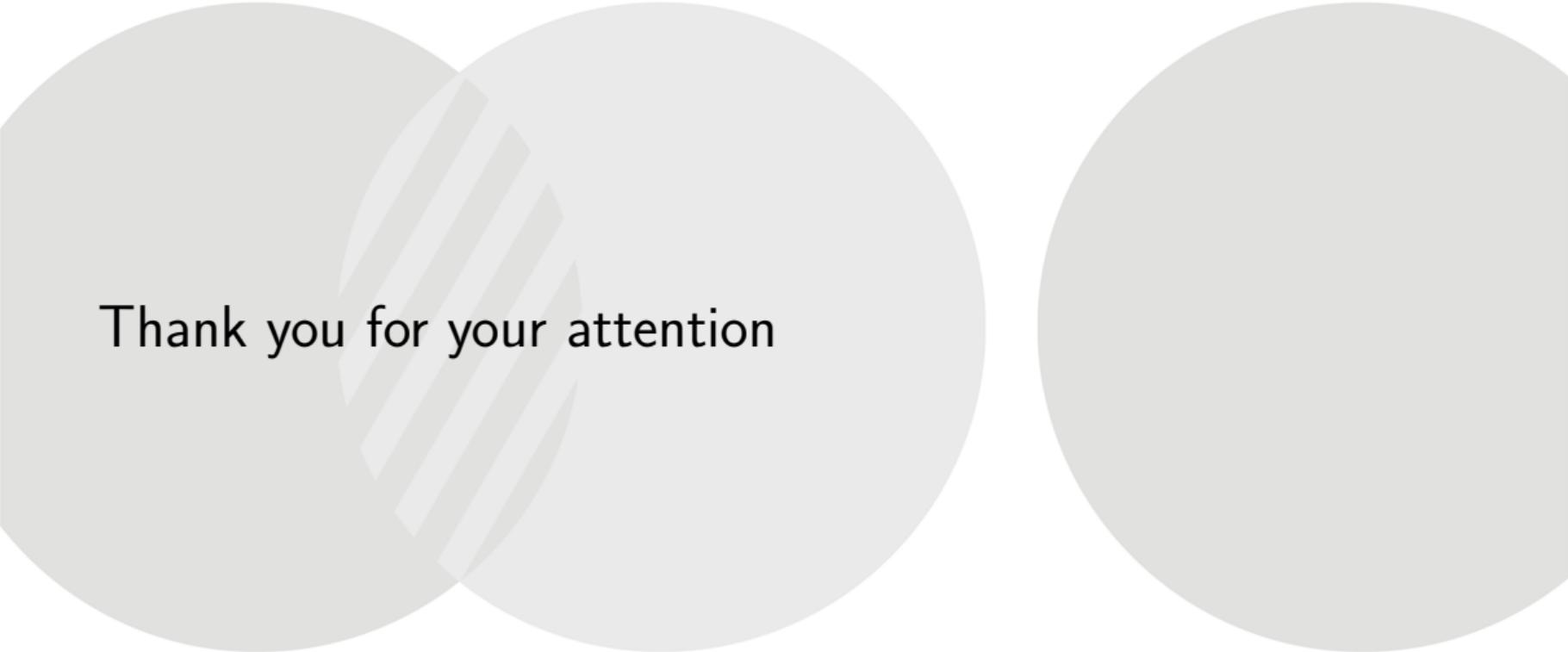
- ▶ Estimates obtained by applying SPREE are consistent with direct estimates at higher levels of spatial aggregation.
- ▶ Compared with the direct estimator, SPREE estimators are characterised by better precision.
- ▶ Statistical data based on administrative registers seem to be a good source of auxiliary variables.
- ▶ The SPREE approach can be used to produce estimates for non-standard territorial domains, such as functional urban areas of provincial capital cities.



Literature

- Józefowski, T. (2022). *Rynek pracy na obszarach funkcjonalnych miast wojewódzkich w świetle estymacji typu SPREE*. PhD thesis, Poznan University of Economics and Business.
- Józefowski, T. Szymkowiak, M. (2013). *Zastosowanie estymatora typu SPREE w szacowaniu liczby osób bezrobotnych w przekroju podregionów*. Studia Oeconomica Posnaniensia, 1(10):120–136.
- Luna Hernandez, A. (2016). *Multivariate Structure Preserving Estimation for Population Compositions*. PhD thesis, University of Southampton.
- Purcell, N. J. Kish, L. (1980). Postcensal Estimates for Local Areas (Or Domains). *International Statistical Review / Revue Internationale de Statistique*, 48(1):3–18.
- Rao, J. M. K. Molina, I. (2015). *Small Area Estimation*. John Wiley and Sons, New Jersey, 2nd edition.
- Zhang, L. C. Chambers, R. L. (2004). Small area estimates for cross-classifications. *Journal of the Royal Statistical Society. Series B: Statistical Methodology*, 66(2):479–496.





Thank you for your attention